

2011 AP[®] STATISTICS FREE-RESPONSE QUESTIONS

3. An apartment building has nine floors and each floor has four apartments. The building owner wants to install new carpeting in eight apartments to see how well it wears before she decides whether to replace the carpet in the entire building.

The figure below shows the floors of apartments in the building with their apartment numbers. Only the nine apartments indicated with an asterisk (*) have children in the apartment.

<table border="1" style="width: 100%; border-collapse: collapse;"> <tr><td style="padding: 2px;">11*</td><td style="padding: 2px;">12</td></tr> <tr><td colspan="2" style="padding: 2px;">1st Floor</td></tr> <tr><td style="padding: 2px;">14</td><td style="padding: 2px;">13</td></tr> </table>	11*	12	1st Floor		14	13	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr><td style="padding: 2px;">21</td><td style="padding: 2px;">22*</td></tr> <tr><td colspan="2" style="padding: 2px;">2nd Floor</td></tr> <tr><td style="padding: 2px;">24</td><td style="padding: 2px;">23*</td></tr> </table>	21	22*	2nd Floor		24	23*	<table border="1" style="width: 100%; border-collapse: collapse;"> <tr><td style="padding: 2px;">31</td><td style="padding: 2px;">32</td></tr> <tr><td colspan="2" style="padding: 2px;">3rd Floor</td></tr> <tr><td style="padding: 2px;">34</td><td style="padding: 2px;">33</td></tr> </table>	31	32	3rd Floor		34	33	
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- (a) For convenience, the apartment building owner wants to use a cluster sampling method, in which the floors are clusters, to select the eight apartments. Describe a process for randomly selecting eight different apartments using this method.
- (b) An alternative sampling method would be to select a stratified random sample of eight apartments, where the strata are apartments with children and apartments with no children. A stratified random sample of size eight might include two randomly selected apartments with children and six randomly selected apartments with no children. In the context of this situation, give one statistical advantage of selecting such a stratified sample as opposed to a cluster sample of eight apartments using the floors as clusters.
4. High cholesterol levels in people can be reduced by exercise, diet, and medication. Twenty middle-aged males with cholesterol readings between 220 and 240 milligrams per deciliter (mg/dL) of blood were randomly selected from the population of such male patients at a large local hospital. Ten of the 20 males were randomly assigned to group A, advised on appropriate exercise and diet, and also received a placebo. The other 10 males were assigned to group B, received the same advice on appropriate exercise and diet, but received a drug intended to reduce cholesterol instead of a placebo. After three months, posttreatment cholesterol readings were taken for all 20 males and compared to pretreatment cholesterol readings. The tables below give the reduction in cholesterol level (pretreatment reading minus posttreatment reading) for each male in the study.

Group A (placebo)

Reduction (in mg/dL)	2	19	8	4	12	8	17	7	24	1
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Mean Reduction: 10.20 Standard Deviation of Reductions: 7.66

Group B (cholesterol drug)

Reduction (in mg/dL)	30	19	18	17	20	-4	23	10	9	22
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Mean Reduction: 16.40 Standard Deviation of Reductions: 9.40

Do the data provide convincing evidence, at the $\alpha = 0.01$ level, that the cholesterol drug is effective in producing a reduction in mean cholesterol level beyond that produced by exercise and diet?